

STATISTICS

Dalarna University



Short-term Forecasting of Reimbursement for Dalarna University

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Abstract

Swedish universities are reimbursed by the government according to a scheme related to the registration of students (HSTK) and the students' performance (HPRK). On a disaggregated level, such as a department or a field, the reimbursement is uncertain as the number and performance of students are fluctuant. So the administration faces the challenge to balance the reimbursement and the expense. In this thesis, we try to distinguish a better forecasting model for the educational fields or the departments of Dalarna University. We analyze the time series by two methods, namely Census II method and the ARIMA method. We apply the two methods to two approaches, direct and indirect approaches. The first one is to use the time series of reimbursement directly; the second one is to forecast the number of students and their performance separately, and then convert these two forecasted values into reimbursement. To compare the results, we choose the indication of MAPE. We use monthly data from Jan. 2000 to Feb. 2008. Finally, we find that, on the department level, the ARMA model of the indirect approach is the best one for forecasting the reimbursement.

Keywords: Census II Method, ARMA Method, MAPE

Contents

| | |
|--|---------------|
| 1. Introduction..... | - 1 - |
| 2. Data Description..... | - 3 - |
| 3. Method | - 5 - |
| 4. Results for the Field of Natural Science | - 6 - |
| 5. Comparison between the Census II Method and the ARMA Method..... | - 11 - |
| 6. Conclusion | - 15 - |
| Reference..... | - 16 - |
| Appendix..... | - 17 - |

1. Introduction

In Sweden, the reimbursement for the higher education sector is always increasing until recently. In 2004, the reimbursement became to decline partly because the educational institutions enrolled less students than before¹ as the reimbursement is highly related to the number and the performance of the college students. To some extent, the reimbursement for a university will fluctuate around a trend. Our thesis is to establish an accurate model to forecast the reimbursement for the fields or the departments in the university. The model may help them to balance their expense and reimbursement better. In this thesis, we take the Dalarna University as an example.

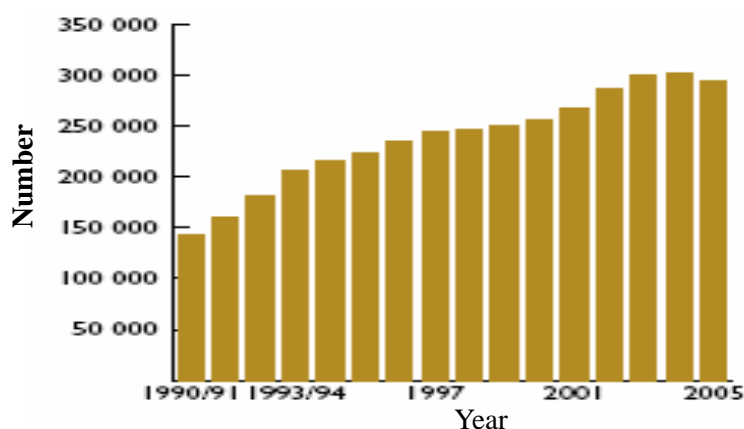


Figure 1: The number of full time equivalent (FTE) students in Sweden
Source: 2005 Annual Report of Swedish National Agency for Higher Education

Figure 1 shows the number of students registered in 1990-2005. In 2005, the total volume of higher education comprised 295,150 full-time students. This is a reduction of 2.5 percent compared with the previous year and this is the first time for twenty years that the number of full-time students declined².

Dalarna University was established in 1977. Today there are about 10 000 students studying

¹ <http://hsv.se/statistics/theannualreport.4.539a949110f3d5914ec800064188.html>

² <http://www.hsv.se/download/18.539a949110f3d5914ec800081527/0638R.pdf>

in this university. Distance education is also offered in various forms. There are more than 200 courses within the areas of welfare, business, infrastructure media, culture and tourism and so on³. All of the courses are classified into 11 fields: the Humanity, Sport, Law, Education, Media, Medicine, Natural Science, Social Science, Technique, Health and Care, and the Others, the amount of the reimbursement depends on these fields. The courses can also be classified into 5 departments: Culture, Social, Health, Humanity, and Industry. The fields and the departments at Dalarna University are shown in Table 1.

Table 1: The share of the fields and departments in terms of the average reimbursement from 2000 to 2008 (%)

| Department \ Field | Culture | Social | Health | Humanity | Industry | Marginal size |
|--------------------|---------|--------|--------|----------|----------|---------------|
| Other | 8.59 | 0.01 | 6.56 | 3.80 | 2.63 | 2.21 |
| Humanity | 5.39 | 0.14 | 0.76 | 55.60 | 0.27 | 7.33 |
| Sport | - | 1.21 | 1.71 | - | - | 0.48 |
| Law | - | 13.07 | 16.90 | - | - | 1.76 |
| Education | 0.83 | 1.96 | 20.86 | 38.96 | 2.69 | 12.00 |
| Media | - | 10.47 | 22.82 | - | - | 16.80 |
| Medicine | 31.31 | - | - | - | - | 4.45 |
| Natural Science | 2.54 | 17.01 | 3.16 | 0.95 | 56.04 | 11.90 |
| Social Science | 11.10 | 42.84 | 19.31 | 1.06 | - | 10.90 |
| Technique | 45.89 | 22.05 | - | - | 40.01 | 21.70 |
| Care | 0.72 | 1.18 | 16.83 | - | - | 10.40 |
| Marginal size | 17.10 | 14.60 | 39.70 | 11.80 | 16.80 | 100.00 |

This table shows the size each field takes up in the departments and the marginal size of the departments and the fields in Dalarna University. For example the field Humanity takes up 5.39 % in the Culture department, and about 7.33 % in this school and the Culture department takes up 17.1 %. From this table we can see the Sport field is the smallest one, whereas the

³ http://du.se/Templates/StartPage_____1622.aspx?epslanguage=SV

Technique field is the largest one.

The key of this thesis is that we classified the data not only by the fields, but also by the departments. To forecast the reimbursement, we choose two approaches: the direct approach and the indirect approach. The first one is to use the time series of the reimbursement directly; the second one is to forecast the number of students and their performance separately and then convert these forecasted values into the reimbursement. We use two methods, namely the Census II method and the ARIMA method, to model these two approaches on the field level and the department level.

2. Data Description

We use the monthly data from Jan. 2000 to Feb. 2008. The Swedish universities are reimbursed by the government according to a simple scheme related to the registration of the students and the student's performance. The allocation rule of the reimbursement is: 60% of the reimbursement is based on the registration and 40% is based on the performance⁴. In this thesis, we use HSTK as the short form for the registration of the students and HPRK for the performance. We get the data of HSTK and HPRK from all the courses. All the courses are classified into 11 fields and how the reimbursement depends on fields is shown in the table A and B of the Appendix C. The HSTK is calculated by the number of registered students multiplying with the credits of the course and dividing by 60 credits which is the total number of credit points for one year full-time study. The calculating method of the HPRK is similar to the HSTK. The only difference is the number of registered students is changed into the number of students who have passed the examination. The two formulations are shown below:

HSTK = number of registered students \times credits of the course /60

HPRK = number of students who have passed the exam \times credits of the course /60

⁴ The Annual Report of Swedish National Agency for Higher Education
<http://hsv.se/statistics/theannualreport.4.539a949110f3d5914ec800064188.html>

We received the data saved in 9 Excel files, which present the 9 years from 2000—2008, and each file contains 12 spreadsheets presenting the 12 months of the year. In each row of the spreadsheet, it lays out the records of the HSTK and HPRK for each course offered by the university.

- **Data classified by fields**

To arrange the data, we merged the records of the courses which belong to the same field in every month by summing these records and named them as THSTK and THPRK. Because the records are accumulative, to get the value of the HSTK and the HPRK happened in this month we should use the one month later data subtract the data of this month. For example, when we calculate the HSTK in the field of Natural Science (NAT) in December 2007, we should use the formulation: $THSTK_{2007,12} - THSTK_{2007,11} = 505.5049 - 502.7699 = 2.735$. To calculate the HPRK in the same field in December 2007, we should use the formulation: $THPRK_{2007,12} - THPRK_{2007,11} = 366.1825 - 320.91 = 45.2725$. With the number of the HSTK and the HPRK of each month in hand, we can convert these values into the monthly reimbursement with the following function:

$$\begin{aligned} \text{Reimbursement} &= 19465 * (THSTK_t - THSTK_{t-1}) + 17085 * (THPRK_t - THPRK_{t-1}) \\ &= 19465 * 2.735 + 17085 * 45.2725 = 826717.438 \end{aligned}$$

Where t represents the months, the 19465 presents the reimbursement for each unit of the HSTK in the field of Natural Science and the 17085 is for each unit of the HPRK, which is shown in Appendix C. The annual total reimbursement of the university is shown in Table 2.

Table 2: The annual reimbursement of Dalarna from 2000-2007 (Million SEK)

| 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 |
|---------|---------|---------|---------|---------|---------|---------|---------|
| 323.923 | 315.706 | 379.360 | 417.720 | 380.854 | 373.210 | 387.713 | 390.240 |

This information presents the trend of the reimbursement, and we can see the fluctuation of the reimbursement during the years. For example in year 2004 the reimbursement is 380.854

million SEK.

- **Data classified by departments**

In the original data, we do not have the level of the reimbursement for departments. To calculate the reimbursement of each department, firstly we merged the records of the courses which belong to the same department in every month, and then in each department we merged the records of the courses which belong to the same field. After these procedures, with the same calculating method for the field just as we stated above, we can get the reimbursement of the department. Then we got the true value happened in every month. Then we had monthly time series data for 9 years for each of the departments.

3. Method

To forecast the reimbursement for one field or one department, we consider two approaches, namely indirect and direct approaches. The reimbursement is determined in a simple way. Let y be the reimbursement of one field or one department, z denotes the number of the HSTK, and w denotes the number of the HPRK. Then we have the formulation:

$$y_t = c_1 * z_t + c_2 * w_t \quad (1).$$

Where the constants c_1 and c_2 are the reimbursement depending on the field and shown in Appendix C. The direct approach is to model \hat{y}_t directly, where \hat{y}_t is a function of past value of y say y_t, y_{t-1}, \dots , and time $t, t-1, \dots$. For the indirect method, first we forecast the z_t and w_t separately, which means we build one model for \hat{z}_t , a function of $z_t, z_{t-1}, \dots, t, t-1, \dots$ and one for the \hat{w}_t , a function of $w_t, w_{t-1}, \dots, t, t-1, \dots$ then convert the two forecasted values into reimbursement calculated by equation (2).

$$\hat{y}_t = c_1 * \hat{z}_t + c_2 * \hat{w}_t \quad (2).$$

Where the " $\hat{\Lambda}$ " means the predicted value. To get the model we choose the Census II

method and the ARIMA method.

Firstly, we introduce the knowledge of the Census II method. Any time series X is composed of trend (T), season (S), cycle (C), and random influences (E). This method is to derive the trend, season, and other components from X . There are two common models:

Multiplicative:
$$X = (T \times C) \times S \times E$$

Additive:
$$X = (T + C) + S + E$$

In this thesis we choose the additive method, because the multiplicative model is commonly used for the growth curve rather than stationary curve. Another reason why we choose the additive model is that the original data contains the 0 value, which can not be transacted by the multiplicative model. The main step of the Census II is computing T+C by moving average and then get S+E=X-(T+C). Then get S by moving average and calculate X-S = T+C+E, the seasonal adjusted value. In this process, we use the moving average many times. Finally we can calculate the value of \hat{X}_t : $\hat{X}_t = \hat{T} + \hat{C} + \hat{S}$. All these steps are performed with statistic software Eviews 3.

We also tried the ARIMA model (Autoregressive Integrated Moving Average model). The main procedure of this model is explained as follow: when we get the observed series, the first thing is to decide if the series is stationary. We use the test of unit root to test if the series is stationary. We found that the data is stationary and hence we need not to difference the series. Then we can construct an ARMA model, and check whether the residuals of the ARMA model are white noise. If not, we repeat the procedure above, if so, the procedure is over.

4. Results for the Field of Natural Science

There are 11 fields and 5 departments in Darlarna University and it would be too many to show all the results. Instead we will describe the modeling process of the field of Natural Science as an example. The proceeding is similar for the other fields and the departments. Summary results are given in sections 5 and 6.

After removing the seasonal factor, we get the seasonal adjusted series of the HSTK in the field Natural Science.

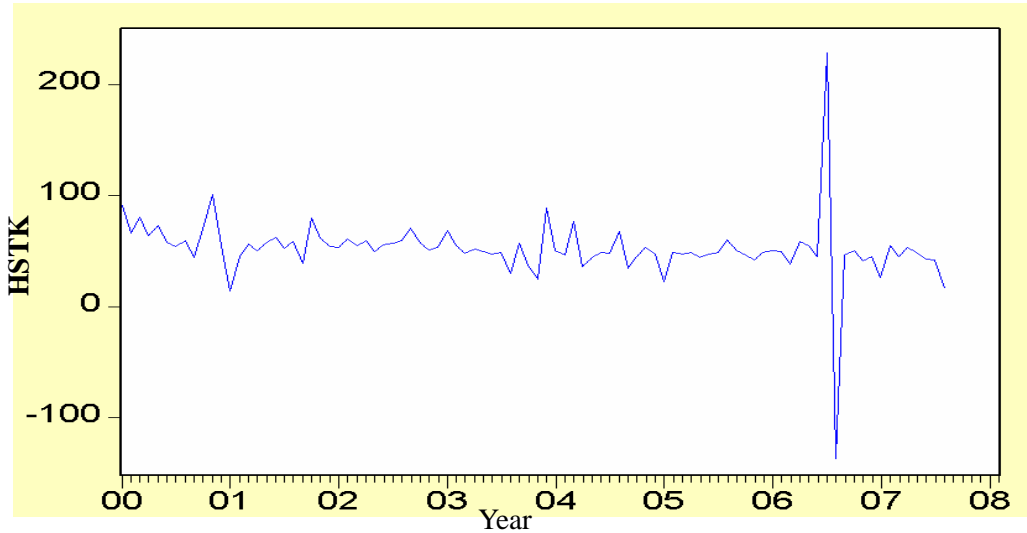


Figure 2: Seasonal adjusted series of the registration in the field Natural Science

Let z_t^* be the seasonal adjusted series. We try several functions to model z_t^* , such as the error function, logistic transform, linear function of t and t^n and log function and so on. In Table 3 we show the AIC for some competing models.

Table 3: The Values of AIC for competing models

| Function | AIC |
|----------------------------------|------|
| Error Function | 9.55 |
| Logistic Transform | 9.58 |
| Linear Function of t and t^n | 9.89 |
| Log Function | 9.85 |

According to AIC, we would like to choose the Error Function:

$$\hat{z}_t^* = b * \frac{2}{\sqrt{\pi}} \int_0^t e^{-z^2} dz + MA(1)$$

This is a function of \hat{z}_t^* and t ; b is a parameter to be estimated. The residuals of the model pass the white noise test. So the model is reasonable. Then we show the graph of seasonal

factor in Figure 3:

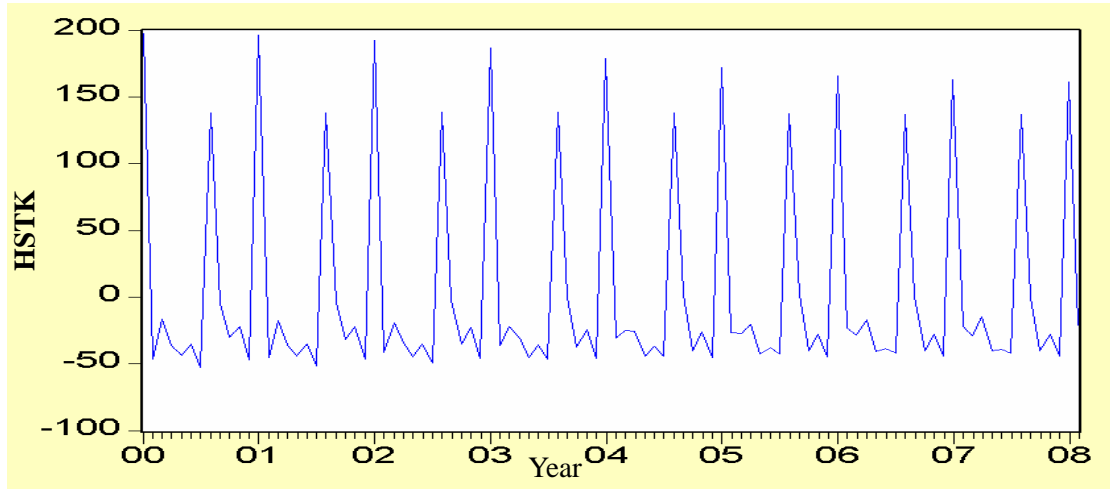


Figure 3: Seasonal factor series of the registration in the field Natural Science

Let z'_t be the seasonal factor series. According to the formulation:

$$\hat{z}_t = \hat{z}_t^* + \hat{z}'_t \quad (3)$$

So we can calculate the value of the \hat{z}_t . Figure 4 shows linear graph of the forecasted data and the original data.

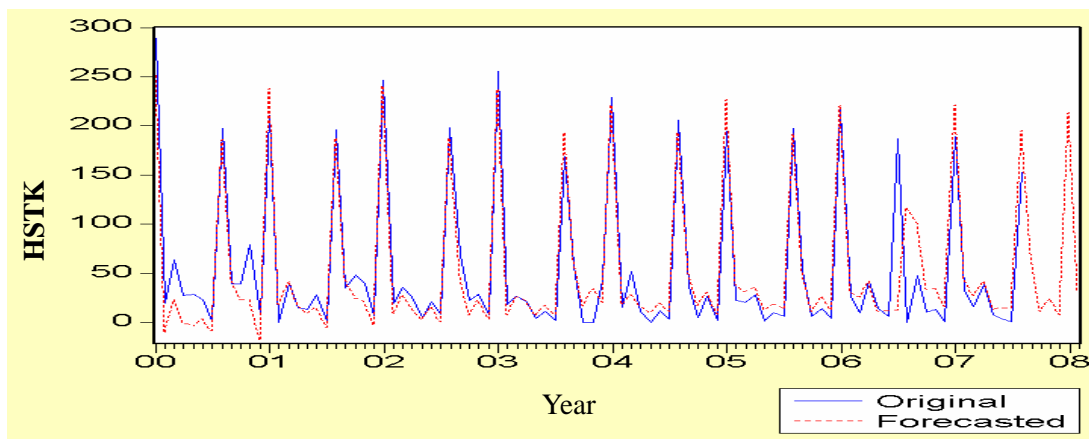


Figure 4: Comparison between original value and forecasted value of the registration in the field Natural Science

The correlation of \hat{z}_t and z_t is 0.92. We also check the index of mean absolute

percentage error (known as MAPE = $\frac{\sum_{t=1}^n |\hat{z}_t - z_t| / z_t}{n} * 100\%$). When n=6, it equals to 22.66 %.

The analysis of the HPRK is similar as the HSTK. Let w_t^* be the seasonal adjusted series, w_t' be the seasonal factor series. The graph of seasonal adjusted is shown below:

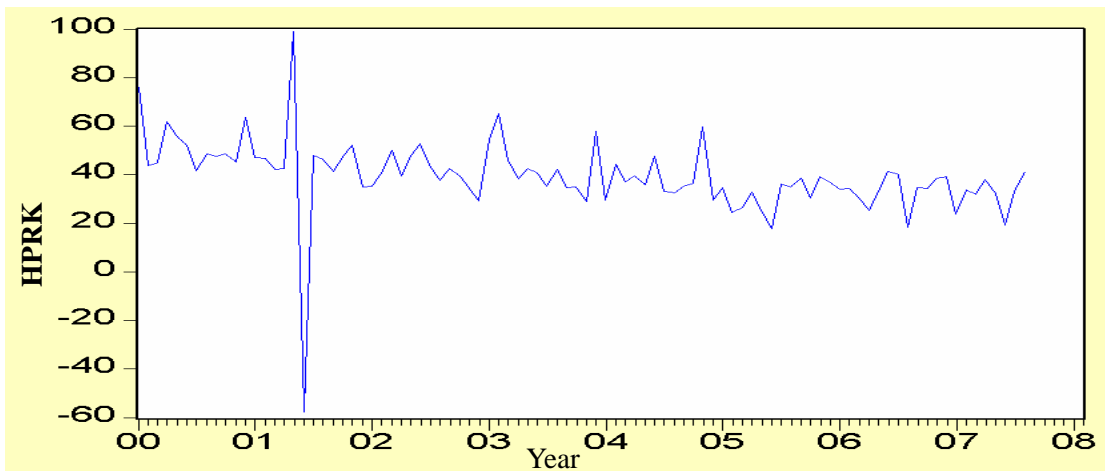


Figure 5: Seasonal adjusted series of performance in the field Natural Science

The result is quite similar as the HSTK. According to AIC, we still choose the error function. Then we show the graph of seasonal factor as follow:

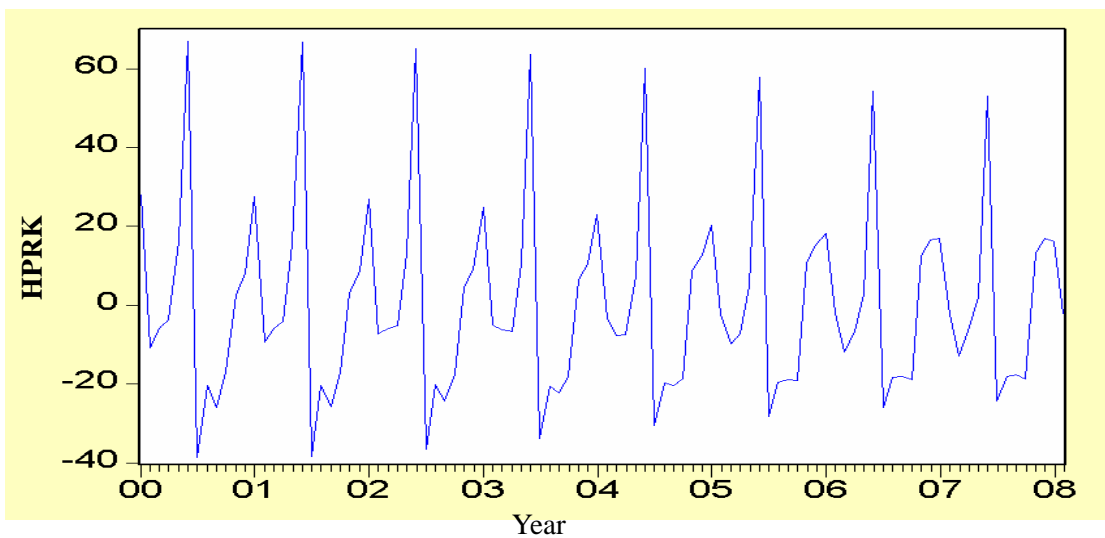


Figure 6: Seasonal factor series of the performance in the field Natural Science

According to the formulation:

$$\hat{w}_t = \hat{w}_t^* + \hat{w}_t' \quad (4)$$

We can get the value of the \hat{w}_t . Figure 7 shows the linear graph of the forecasted data and the original data.

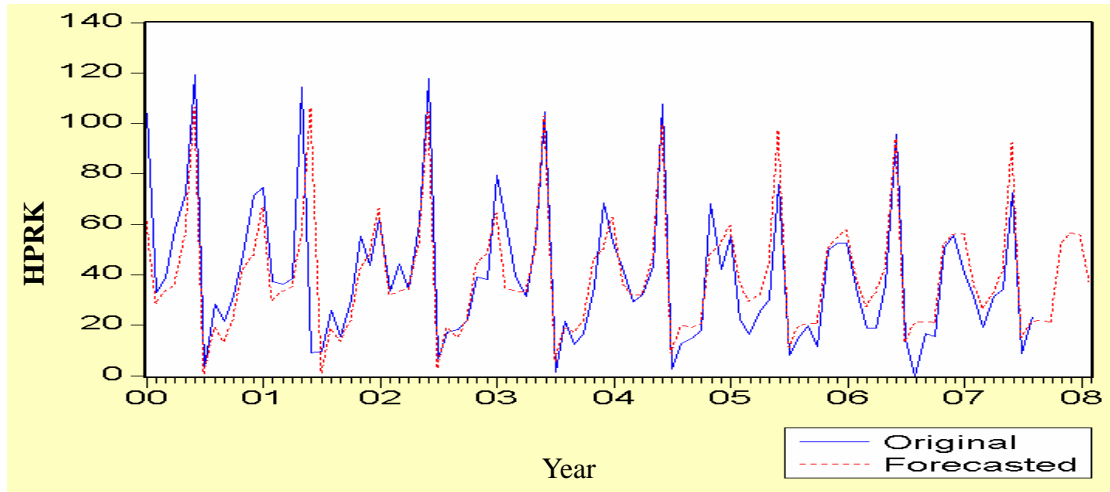


Figure 7: Comparison between the original value and the forecasted value of the performance in the field Natural Science

The mean absolute percentage error is 39.55 %. Then totally reimbursement of the field Natural Science can be calculated by the function:

$$\hat{y}_t = c_1 * \hat{w}_t + c_2 * \hat{z}_t \quad (c_1 = 44\,706, c_2 = 37\,702).$$

Figure 8 shows the forecasted series of the reimbursement.

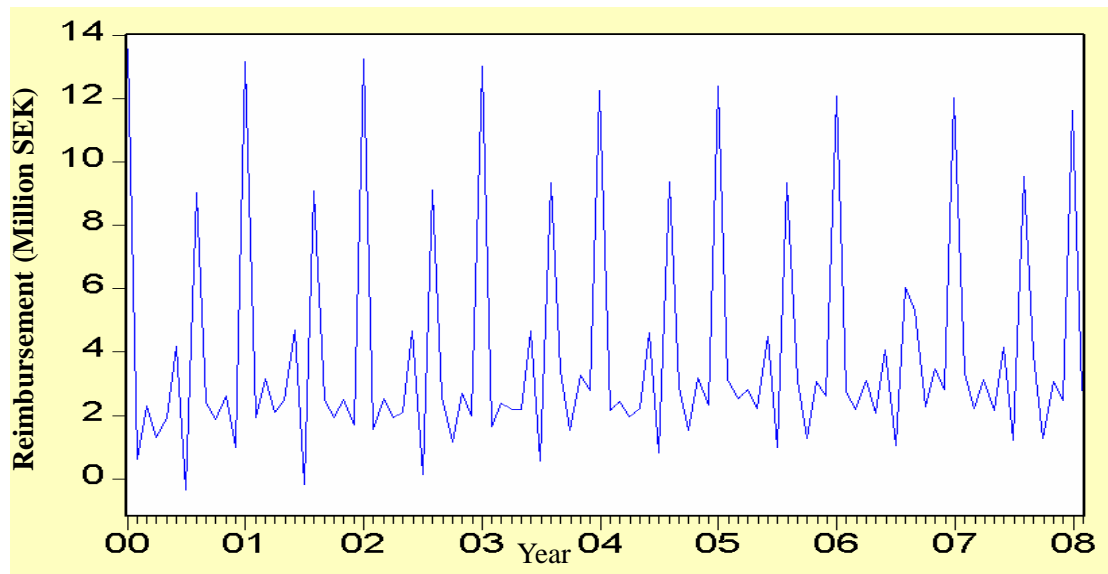


Figure 8: Forecasted series of the reimbursement in the field Natural Science

With the similar analysis for the other fields, we can get the total reimbursement of Dalarna University by summing the reimbursement of the 11 fields. The result has been shown in the next section. The analysis with the direct approach is quite similar as the indirect approach. We just model time series \hat{y}_t directly. So we will show the comparison of the forecasted results in the next section. The analysis of the departments is also similar. Still the results will be shown in the section 5.

5. Comparison between the Census II Method and the ARMA Method

To compare which method is better on these two approaches and two levels, we choose the MAPE as an indication. Obviously the smaller the MAPE is, the better the model should be. To find out if there are some differences in short-term forecasting between the methods and the approaches on the two levels, we estimated three different forecasting lengths of 3 months, 6 months and 12 months. In order to make the results comparable, we give the predictions from Mar. 2007 to Feb. 2008. Take 3 months forecasting as an example; first we deem the data interval from Jan. 2000- Feb. 2007 as a set $\{A\}$. For the first 3month forecasting of Mar. 2007-May 2007, we use the set $\{A\}$. Then we use $\{A\}$ + the original data of Mar. 2007-May

2007 to forecast the data of Jun. 2007-Aug. 2007. We use {A} + the original data of Mar. 2007-Aug. 2007 to forecast Sep. 2007-Nov. 2007. Finally, we forecast Dec. 2007-Feb. 2008 by the set {A} + the original data of Sep. 2007-Nov. 2007. After the steps above, we calculate the MAPE of the forecasted data from Mar. 2007-Feb. 2008. The results from Census II method are shown in the table below. We compare the results on the field level. Then we compare results on the department level in the similar way.

Table 4: Comparison in terms of MAPE between the direct and indirect approaches with the data classified by fields where the Census II is used for forecasting (%)

| Field \ Period | Direct Approach | | | Indirect Approach | | |
|-----------------|-----------------|----------|-----------|-------------------|----------|-----------|
| | 3 months | 6 months | 12 months | 3 months | 6 months | 12 months |
| Other | 42.27 | 48.07 | 48.51 | 42.64 | 49.15 | 50.37 |
| Humanity | 32.41 | 33.54 | 35.94 | 32.89 | 37.28 | 38.73 |
| Sport | 92.39 | 104.27 | 109.51 | 116.41 | 130.40 | 143.03 |
| Law | 30.00 | 38.69 | 43.56 | 34.29 | 40.76 | 45.25 |
| Education | 27.44 | 34.43 | 37.52 | 27.37 | 35.89 | 37.92 |
| Media | 30.52 | 39.48 | 46.50 | 36.07 | 44.72 | 46.86 |
| Medicine | 21.38 | 22.54 | 24.94 | 22.93 | 23.19 | 25.68 |
| Natural Science | 27.98 | 32.38 | 35.49 | 33.54 | 37.38 | 39.94 |
| Social Science | 21.95 | 22.45 | 25.08 | 24.25 | 26.97 | 27.35 |
| Technique | 36.02 | 38.68 | 38.85 | 36.27 | 38.21 | 39.94 |
| Health Care | 27.81 | 31.23 | 34.35 | 27.95 | 34.36 | 34.49 |
| Average MAPE | 29.78 | 34.15 | 37.07 | 31.82 | 36.79 | 38.65 |

Because the Sport field is a quite small field and the data are too few to forecast, so we can ignore the effect it made. The Average MAPE is the average of all the fields except Sport.

Table 5: Comparison in terms of MAPE between the direct and indirect approaches with data classified by departments where the Census II is used for forecasting (%)

| Period Department | Direct Approach | | | Indirect Approach | | |
|----------------------|-----------------|----------|-----------|-------------------|----------|-----------|
| | 3 months | 6 months | 12 months | 3 months | 6 months | 12 months |
| Culture | 30.60 | 35.87 | 36.51 | 32.60 | 37.32 | 39.94 |
| Social | 29.61 | 32.09 | 33.75 | 27.59 | 36.61 | 37.88 |
| Health | 27.15 | 32.97 | 35.65 | 29.54 | 33.54 | 37.68 |
| Humanity | 31.96 | 35.35 | 40.85 | 32.38 | 36.41 | 41.77 |
| Industry | 29.05 | 33.35 | 35.92 | 31.18 | 36.84 | 38.39 |
| Average MAPE | 29.67 | 33.93 | 36.54 | 30.66 | 36.14 | 39.13 |

From Table 4 and Table 5, on the average level, we can conclude the direct approach is better than the indirect approach. While the data classified by departments do some help to get a more accurate prediction than the data classified by fields. As mentioned above, in this thesis, we also tried the ARMA model. The results are shown in tables 6 and 7:

Table 6: Comparison in terms of MAPE between the direct and indirect approaches with data classified by fields where the ARMA is used for forecasting (%)

| Period Fields | Direct Approach | | | Indirect Approach | | |
|------------------|-----------------|----------|----------|-------------------|----------|-----------|
| | 3 months | 6 months | 12months | 3 months | 6 months | 12 months |
| Other | 38.62 | 44.53 | 46.76 | 41.12 | 45.76 | 49.96 |
| Humanity | 25.45 | 28.96 | 34.92 | 27.31 | 30.11 | 35.36 |
| Sport | 57.06 | 66.37 | 70.83 | 57.50 | 69.59 | 72.09 |
| Law | 32.30 | 41.45 | 44.16 | 36.06 | 41.64 | 45.15 |
| Education | 25.82 | 30.63 | 31.85 | 27.23 | 31.85 | 32.75 |
| Media | 34.04 | 41.36 | 45.59 | 37.04 | 44.19 | 45.33 |
| Medicine | 27.55 | 29.97 | 35.99 | 27.38 | 31.09 | 34.25 |
| Natural Science | 24.80 | 35.17 | 35.41 | 25.68 | 30.92 | 35.77 |
| Social Science | 22.10 | 27.27 | 28.52 | 22.99 | 28.51 | 29.44 |
| Technique | 26.38 | 30.68 | 33.88 | 27.47 | 31.62 | 34.84 |
| Health Care | 21.09 | 27.89 | 28.96 | 22.47 | 27.94 | 29.57 |
| Average MAPE | 27.82 | 32.60 | 36.60 | 29.48 | 34.36 | 37.24 |

Table 7: Comparison in terms of MAPE between the direct and indirect approaches with data classified by departments where the ARMA is used for forecasting (%)

| Period Department | Direct Approach | | | Indirect Approach | | |
|----------------------|-----------------|----------|-----------|-------------------|----------|-----------|
| | 3 months | 6 months | 12 months | 3 months | 6 months | 12 months |
| Culture | 25.49 | 34.24 | 36.45 | 24.24 | 34.87 | 35.23 |
| Social | 27.29 | 29.90 | 34.66 | 27.08 | 28.78 | 35.02 |
| Health | 27.51 | 31.23 | 35.01 | 25.16 | 30.17 | 35.72 |
| Humanity | 28.06 | 35.15 | 41.26 | 27.80 | 34.60 | 39.07 |
| Industry | 28.19 | 30.81 | 34.67 | 26.89 | 29.02 | 30.26 |
| Average MAPE | 27.31 | 32.27 | 36.41 | 26.23 | 31.49 | 35.06 |

Compared with the table 6 and table 7, again we get the conclusion that the forecasting result from the department level is better than the result from the field level. From the table 6, on average, the direct approach is also better than the indirect approach as mentioned in analysis of Census II. But it shows an opposite situation in table 7, the indirect approach achieves a better result. Compared with Census II method, the ARMA method seems to achieve a better result, no matter which approaches are applied to.

6. Conclusion

Judging from the rule that the smaller the MAPE is the better the forecasting result should be, we get the conclusion that on the average level, the indirect approach with the ARMA method and classify data on the department level achieves a better result. That is to say, to give a more accurate forecasting reimbursement of Dalarna University we had better try this path rather than the other paths. We analyze the reason why the ARMA model is better than the Census II method. As we have mentioned, Census II method puts emphasis on showing trend, season, circle and error. It decomposes the time series into these four components, but it is hard to give an accurate decomposition for the four parts. What's more, dealing with the data with the moving average method for too many times may lead to the reduction of the length of the time series. Compared with the Census II method, the ARMA method can make up these deficiencies. In addition, ARMA method pays more weights to the recent data, which means the forecasted result could be closer to the reality.

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Appendix

Appendix A: Example of Original data of HSTK in Natural Science Field

| Period | observation | Period | observation | Period | observation |
|--------|-------------|--------|-------------|--------|-------------|
| 2000 | | 2003 | | 2006 | |
| 1 | 288.8844 | 37 | 255.41563 | 73 | 216.6725 |
| 2 | 19.825 | 38 | 18.49062 | 74 | 25.7425 |
| 3 | 63.7 | 39 | 26.33438 | 75 | 9.975 |
| 4 | 27.55 | 40 | 21.09999 | 76 | 41.975 |
| 5 | 28.95 | 41 | 4.125 | 77 | 13.975 |
| 6 | 22.7875 | 42 | 11.41251 | 78 | 6.375 |
| 7 | 1.4 | 43 | 2.15625 | 79 | 186.6656 |
| 8 | 197.45 | 44 | 168.65622 | 80 | 0 |
| 9 | 39.4375 | 45 | 57.1438 | 81 | 47.4038 |
| 10 | 39.4187 | 46 | 0 | 82 | 10.1544 |
| 11 | 78.9688 | 47 | 0 | 83 | 13.595 |
| 12 | 7.55 | 48 | 43.3225 | 84 | 0.635 |
| 2001 | | 2004 | | 2007 | |
| 13 | 210.4812 | 49 | 229.17375 | 85 | 189.315 |
| 14 | 0 | 50 | 15.63755 | 86 | 32.7187 |
| 15 | 38.8626 | 51 | 51.4249 | 87 | 15.7313 |
| 16 | 14.475 | 52 | 10.8188 | 88 | 38.525 |
| 17 | 13.025 | 53 | 0 | 89 | 7.8025 |
| 18 | 27.6499 | 54 | 11.88 | 90 | 3.5 |
| 19 | 1.175 | 55 | 3.705 | 91 | 0.42407 |
| 20 | 196.3001 | 56 | 205.5031 | 92 | 153.44006 |
| 21 | 34.7749 | 57 | 36.1182 | 93 | 24.64502 |
| 22 | 48.1688 | 58 | 4.705 | 94 | 23.98663 |
| 23 | 39.45 | 59 | 26.6999 | 95 | 12.68166 |
| 24 | 7.1875 | 60 | 2.03 | 96 | 2.73499 |
| 2002 | | 2005 | | 2008 | |
| 25 | 246.2875 | 61 | 194.52 | 97 | 190.7245 |
| 26 | 19.3063 | 62 | 22.2312 | 98 | 25.24918 |
| 27 | 35.4374 | 63 | 20.0688 | | |
| 28 | 25.5376 | 64 | 28.175 | | |
| 29 | 4.7812 | 65 | 1.175 | | |
| 30 | 20.7875 | 66 | 9.43 | | |
| 31 | 8.2 | 67 | 6.425 | | |
| 32 | 198.05 | 68 | 197.405 | | |
| 33 | 68.6062 | 69 | 52.4487 | | |
| 34 | 22.275 | 70 | 6.0751 | | |
| 35 | 28.6501 | 71 | 14.1975 | | |
| 36 | 7.3187 | 72 | 3.8849 | | |

Appendix B: Example of Original data of HPRK in Natural Science Field

| Period | observation | Period | observation | Period | observation |
|--------|-------------|--------|-------------|--------|-------------|
| 2000 | | 2003 | | 2006 | |
| 1 | 104.0406 | 37 | 79.54375 | 73 | 52.41625 |
| 2 | 33.00937 | 38 | 60.18745 | 74 | 32.3225 |
| 3 | 38.9031 | 39 | 39.43755 | 75 | 18.83875 |
| 4 | 58.0988 | 40 | 31.51125 | 76 | 18.6969 |
| 5 | 72.0194 | 41 | 53.0612 | 77 | 36.07873 |
| 6 | 119.2481 | 42 | 104.4782 | 78 | 95.72749 |
| 7 | 2.86875 | 43 | 1.40623 | 79 | 14.1875 |
| 8 | 28.24687 | 44 | 21.45937 | 80 | 0 |
| 9 | 21.50825 | 45 | 12.3625 | 81 | 16.60688 |
| 10 | 31.72865 | 46 | 16.7438 | 82 | 15.61125 |
| 11 | 47.9399 | 47 | 35.2412 | 83 | 50.81375 |
| 12 | 71.6524 | 48 | 68.5662 | 84 | 55.5775 |
| | 2001 | | 2004 | | 2007 |
| 13 | 74.52187 | 49 | 52.70875 | 85 | 40.69375 |
| 14 | 37.16873 | 50 | 41.07188 | 86 | 31.3275 |
| 15 | 36.3938 | 51 | 29.3675 | 87 | 19.035 |
| 16 | 38.34997 | 52 | 32.11625 | 88 | 31.46755 |
| 17 | 114.5139 | 53 | 43.29124 | 89 | 34.2912 |
| 18 | 9.0374 | 54 | 107.825 | 90 | 72.325 |
| 19 | 9.6903 | 55 | 2.4663 | 91 | 8.6517 |
| 20 | 25.909 | 56 | 12.7625 | 92 | 23.3783 |
| 21 | 15.5581 | 57 | 14.7906 | 93 | 10.6825 |
| 22 | 30.1125 | 58 | 17.77 | 94 | 12.2567 |
| 23 | 55.2988 | 59 | 68.30375 | 95 | 36.8008 |
| 24 | 74.52187 | 60 | 42.25375 | 96 | 45.2725 |
| 2002 | | 2003 | | 2008 | |
| 25 | 43.6511 | 61 | 54.91875 | 97 | 53.09418 |
| 26 | 62.3115 | 62 | 22.25125 | 98 | 22.44625 |
| 27 | 33.4825 | 63 | 16.475 | | |
| 28 | 44.3813 | 64 | 25.54375 | | |
| 29 | 34.0987 | 65 | 30.24685 | | |
| 30 | 60.8406 | 66 | 75.6825 | | |
| 31 | 117.8094 | 67 | 8.025 | | |
| 32 | 6.4625 | 68 | 15.2913 | | |
| 33 | 17.4375 | 69 | 19.81 | | |
| 34 | 18.0813 | 70 | 11.4937 | | |
| 35 | 22.0781 | 71 | 49.8388 | | |
| 36 | 38.9832 | 72 | 52.4087 | | |

Appendix C: Different Reimbursement Level for Different Science Field

Table A (HSTK) – registration (SEK)

| Field | | Amount |
|-----------------|----|---------|
| Humanity | HU | 19 465 |
| Sport | ID | 89 681 |
| Law | JU | 19 465 |
| Education | LU | 29 719 |
| Medicine | MD | 50 875 |
| Media | ME | 260 810 |
| Natural Science | NA | 44 706 |
| Social Science | SA | 19 465 |
| Technique | TE | 44 706 |
| Health Care | VÅ | 45 527 |
| Other | ÖV | 35 903 |

Table B: (HPRK) - performance (SEK)

| Field | | Amount |
|-----------------|----|---------|
| Humanity | HU | 17 085 |
| Sport | ID | 42 895 |
| Law | JU | 17 085 |
| Education | LU | 35 385 |
| Medicine | MD | 63 924 |
| Media | ME | 211 087 |
| Natural Science | NA | 37 702 |
| Social Science | SA | 17 085 |
| Technique | TE | 37 702 |
| Health Care | VÅ | 40 299 |
| Other | ÖV | 29 165 |